# Polycrystalline Diffraction 

Matt Miller<br>Sibley School of Mechanical and Aerospace Engineering Cornell High Energy Synchrotron Source (CHESS)<br>Cornell University



Cornell High Energy
Synchrotron Source
Cornell University
College of Engineering

## Where's Cornell?



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## Fingerlakes AVA Wine Region (American Viticultural Area)



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## Ithaca is Gorges



Ithaca Falls


Taughannock Falls

## Cornell Campus - Ithaca



## Cornell Camnus - Ithaca



## CHESS

## The Cornell High Energy Synchrotron Source



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- CHESS
- 1 of 2 high energy storage rings in the U.S.
- Funded by the U.S. National Science Foundation
- Accelerator research since 1934



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- Now it is only there to make $x$-rays



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- Complementary to DOE
- $20 \%$ new users
- Educational mission
- Cornell influence
- People - "can do" mindset



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- CHESS-U\&2019 Renewal

G-lines, 2002

Synchrotron

Linac Converter

$$
\begin{aligned}
& \text { CHESS West (A, B, C) } \\
& \text { 1979, several }
\end{aligned}
$$

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Synchrotron
$e^{+}$
Transfer Line

G-lines, 2002


Storage Ring
$\qquad$
ce


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- New funding model....


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CESR



- Reconfigure for 1 direction running
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## The World's High Energy Synchrotrons

## APS - Chicago


http://www.anl.gov

SPring-8 - Japan

http://www.riken.jp

ESRF - Grenoble

http://www.esrf.eu

Petra-III - Hamburg

http://http://photon-science.desy.de

CHESS


## Outline

- Our Motivation
- Quick diffraction primer
- Examples
- A New CHESS
- Directions
- Tips


## Our Motivation for Exploring High Energy X-ray Diffraction

## Our Motivation for Exploring High Energy X-ray Diffraction

- Material Structure and Behavior


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Ti-6-4

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- Component design (performance)
- Material design (processing)


Ti-6-4

## Hope: Microstructure-Based Modeling

Owen Richmond (US Steel, Alcoa), 1985

```
STRUCTURAL SCALES
```

SCALE
continuum
Polyphase $\left(10^{-2}\right)$

Polycrystal ( $10^{-4}$ )

Crystal (10-6)
Slip System $\left(10^{-8}\right)$
Dislocation $\left(10^{-10}\right)$

Structural Objects

$$
\begin{aligned}
& \text { Phases } \\
& \text { Crystals } \\
& \text { Slip Sytems } \\
& \text { Dislocation } \\
& \text { Networks } \\
& \text { Atoms }
\end{aligned}
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Polycrystal (10-4) Crystals


Structural Objects
Polycrystal" Models


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## Hope: Microstructure-Based Modeling

- Multiscale modeling research is "rampant" - very little crystal scale mechanical testing data, however
-Overarching idea: use High Energy X-ray Diffraction (HEXD) data and in situ loading with FEM representation of microstructure to understand crystal scale material behavior - Processing and Performance - induced CHANGES in unit cell to understand material response
- Merge model with diffraction data:
M.P. Miller and PR. Dawson, Current Opinion in Solid State \& Materials Science, 18, 286-299, 2014.


## Instructional Videos From CHESS

- Google: Chess x-ray micromechanics
- https://www.youtube.com/watch?v=kYEboNz423A\&t=9s



## MAE 7110 Course Notes

1 Some Elements of Solid Mechanics ..... 3
1.1 Direct Notation ..... 3
1.2 Indicial Notation ..... 3
1.3 Coordinate Transformations ..... 5
1.4 Stress and Strain ..... 6
2 Crystallography, Orientations and Symmetry ..... 7
2.1 Basic Crystallography ..... 7
2.2 Orientations ..... 13
2.3 Symmetry ..... 19
3 Elements of Bragg Diffraction ..... 25
3.1 X-rays and Waves ..... 25
3.2 Bragg's Law ..... 28
3.3 X-Ray Absorption ..... 29
4 The Laue Equations and The Rotating Crystal Experiment ..... 31
4.1 Scattering from an Electron ..... 31
4.2 The Scattering Vector ..... 33
4.3 Scattering from an Atom ..... 34
4.4 Scattering from a Crystal (Diffraction) ..... 35
4.5 Ewald's Sphere ..... 38
4.6 Rotating Crystal Diffraction Experiments ..... 40

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- You need to understand diffraction (or scattering) well enough to do your science - the deeper your understanding, the more versatile the tool will be for you.


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- Connecting $x$-ray data to underlying material behavior is challenge and the opportunity.
- Obtaining in situ (real time) information over an entire polycrystalline aggregate is the main advantage of doing diffraction at a light source
- Be careful, it is easy to get "hooked" on diffraction and light sources and late nights and multiple days at the beam line and the tool becomes your science... it's actually pretty great!


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1. Diffracting Crystal
2. Area Detector
3. Debye-Scherrer Ring

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- Collect a field of data
- Slits enable stepping through $T$


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F
https://en.wikipedia.org/wiki/ File:EDXRD_Schematic.png\#/media/

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- iransiate sampie ana/or aetector
- Collect a field of data
- Slits enable stepping through $T$
- SERIOUS fast alternative to neutron diffraction


## Beam size / grain size: Powder or Single Crystal



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- MultiGrain Experiments (Spots)
- Collect diffracted intensity in each grain
- 100s to 2000 grains
- Detector distance
- Near field - orientation map of polycrystal
- Fare field - strains and evolution with insitu loading


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## High Energy X-ray diffraction (HEXD) Detector Distances

1 m

## Near Field

 Grain Maps Lattice Strain (Tensor) and Orientations of each crystalVery Far Field
High Resolution Strain and Orientation

Real Space Resolution

Reciprocal Space
Resolution

Better Reciprocal Space Resolution

## Lattice Strains - Link to Stress



## Lattice Strains - Link to Stress

- Start with the idea of stress analysis using resistance strain gages


$$
\begin{aligned}
\epsilon_{A}\left(\theta_{A}\right) & =\cos ^{2}\left(\theta_{A}\right) \epsilon_{11}+\sin ^{2}\left(\theta_{A}\right) \epsilon_{22}+2 \sin \left(\theta_{A}\right) \cos \left(\theta_{A}\right) \epsilon_{12} \\
\epsilon_{B}\left(\theta_{B}\right) & =\cos ^{2}\left(\theta_{B}\right) \epsilon_{11}+\sin ^{2}\left(\theta_{B}\right) \epsilon_{22}+2 \sin \left(\theta_{B}\right) \cos \left(\theta_{B}\right) \epsilon_{12} \\
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- Plane Stress - 3 Strains


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- Start with the idea of stress analysis using resistance strain gages
- Plane Stress - 3 Strains
- Rosette Equations for the strain tensor



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- Start with the idea of stress analysis using resistance strain gages
- Plane Stress - 3 Strains
- Rosette Equations for the strain tensor
- Crystal lattice strains and rotates under applied load
- Change in $2 \theta$ produces a peak shift = normal strain


SGT-1/350-TY11

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\epsilon_{A}\left(\theta_{A}\right) & =\cos ^{2}\left(\theta_{A}\right) \epsilon_{11}+\sin ^{2}\left(\theta_{A}\right) \epsilon_{22}+2 \sin \left(\theta_{A}\right) \cos \left(\theta_{A}\right) \epsilon_{12} \\
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\epsilon_{C}\left(\theta_{C}\right) & =\cos ^{2}\left(\theta_{C}\right) \epsilon_{11}+\sin ^{2}\left(\theta_{C}\right) \epsilon_{22}+2 \sin \left(\theta_{C}\right) \cos \left(\theta_{C}\right) \epsilon_{12}
\end{aligned}
$$

## Lattice Strains - Link to Stress

- Start with the idea of stress analysis using resistance strain gages
- Plane Stress - 3 Strains
- Rosette Equations for the strain tensor
- Crystal lattice strains and rotates under applied load
- Change in $2 \theta$ produces a peak shift = normal strain



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SGT-1/350-TY11

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$$
\begin{aligned}
& \epsilon_{A}\left(\theta_{A}\right)=c c \\
& \epsilon_{B}\left(\theta_{B}\right)=c c \mathrm{CeO}_{2}\{311\} \\
& \epsilon_{C}\left(\theta_{C}\right)=c c
\end{aligned}
$$




- Mechanics: equilibrium and 6 strains


## High Energy X-ray Diffraction at CHESS \& APS sector 1

## High Energy X-ray Diffraction at CHESS \& APS sector 1



CHESS A2-2003

## High Energy X-ray Diffraction at CHESS \& APS sector 1



CHESS A2-2003


## High Energy X-ray Diffraction at CHESS \& APS sector 1



CHESS A2-2003


A2-2010

## High Energy X-ray Diffraction at CHESS \& APS sector 1



CHESS A2-2003


A2-2010

## A2-2013

High Energy X-ray Diffraction at CHESS \& APS sector 1


Cornell University
Cornell High Energy Synchrotron Source

## High Energy X-ray Diffraction at CHESS \& APS sector 1



High Energy X-ray Diffraction at CHESS \& APS sector 1


## Tensile Response of One Crystal - Far Field



## Tensile Response of One Crystal - Far Field



Sample stress state is uniaxial
Crystal stress state is NOT uniaxial Model captures this behavior in most crystals for uniaxial loading


Wong et. al, 2013, Comp. Mat. Sci., 77, 456-466.


## Cyclic Deformation of High Purity Copper




- Fatigue Crack initiation in copper
- Heterogeneous plastic slip
- Cyclic tests:
- OFHC (99.9\% pure copper)
- CHESS F2 \& APS 1-ID
- Su Leen Wong \& Robert Carson simulations (P. Dawson)

Macroscale Stress-Strain

## Forward projection: interface with the model



## Forward projection: interface with the model



## Forward projection: interface with the model



## Forward projection: interface with the model

Forward Projection / Virtual Diffractometer

- Put diffraction model into FEM
- Accurately represent $x$-ray paths and detector
- Distortion and orientation of virtual crystals within virtual diffraction data
- Compare virtual and real detectors directly
- Hypothesis investigation
- See impact directly



## Diffracted Intensity Distribution - Far Field Detector

before macroscopic yield

- Polycrystal Sample - rotate in $\omega$
- 100-1000 grains
- 20-100 peaks per grain
- Each peak contains a projection of strain and orientation distributions within a grain
- Post-yield "smearing" associated with plasticity - crystallographic slip
- To first approximation
- Orientation spread: $\eta$ (azimuthal) \&w
- Strain spread: $2 \theta$ (radial) - traditional line broadening
- Moments of intensity distribution
- Mean value (centroid)
- Full Width Half Max (spread)

after macroscopic yield



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before macroscopic yield



## Finite Element Model - Virtual

 intensity projected onto detector (1)


## Finite Element Model - Virtual



## Orientation and Strain Spread



- From each peak (spot) extract simple center of mass (COM) and spread (FWHM) information
- Radial - lattice strain
- Azimuthal - orientation
- Using all spots for 1 crystal (20-100), compute $\Theta$ and $\zeta$

$$
\begin{gathered}
\left(\Delta \eta_{i}^{F W H M}\right)_{n}=\left(\eta_{i}^{F W H M}\right)_{n}-\left(\eta_{0}^{F W H M}\right)_{n} \\
\zeta=\frac{1}{N} \sum_{n=1}^{N}\left(\Delta \eta_{i}^{F W H M}\right)_{n}
\end{gathered}
$$

Orientation
$\left(\Delta 2 \theta_{i}^{F W H M}\right)_{n}=\left(2 \theta_{i}^{F W H M}\right)_{n}-\left(2 \theta_{0}^{F W H M}\right)_{n}$
$\Theta=\frac{1}{N} \sum_{n=1}^{N}\left(\Delta 2 \theta_{i}^{F W H M}\right)_{n}$
Lattice Strain

## Evolution of $\zeta$




## $\zeta$ Distribution over the aggregate





Experiment


Model

## $\boldsymbol{\Phi}$ Distribution (strains)



## InSit $\mu$ @CHESS

- Push the envelope of High Energy X-ray Diffraction (HEXD) methods
- Create new methods, steal others
- Provide "enhanced support" of HEXD experiments
- Meet designers, scientists, non-x-ray experts "half way"
- Model and analysis support
- Form partnerships: industry, national labs, university faculty
- Spectrum of Methods and Applications
- Residual Stress
- Thick sections
- Stress + chemistry


CAT - First Beamtime Fall 2014

- AM parts
- In situ Fatigue Crack Growth
- Other In situ conditions


## InSit $\mu$ People

- Armand Beaudoin: InSit $\mu$ Associate Director, UIUC emeritus Prof., distinguished industrial career, experiment/model interface
- Darren Pagan: Staff scientist, novel HEXD methods / data analysis / upgrade
- Chris Budrow: CHESS GRA working on residual stress
- Ramya Nair: Post-Doc: working on fracture in cement
- Kelly Nygren: Post-Doc: blending EM and HEXD
- Eric Miller: Tufts ECE Prof., signal processing, data science



## Fatigue crack growth - Aluminum



## 35k cycles



## FCG in Ti-6-4 (Pilchak)



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## FCG in Ti-6-4 (Pilchak)



# Welding Residual Stress Measurement Results 

Justin Mach, Senior Engineer, Caterpillar<br>Armand Beaudoin, Industrial Llaison, InSitu@CHESS<br>Matt Miller, Director, InSit $@$ CHESS<br>Darren Dale, CHESS F2 Beamline Scientist / Associate Director, InSit $\mu$ @CHESS<br>Peter Ko, CHESS Research Associate<br>Graduate Research Assistants (Cornell University): Darren Pagan, Mark Obstalecki, \& Chris Budrow<br>Graduate Research Assistant (University of Illinois at Urbana-Champaign): Kamalika Chatterjee

## Lap Joint Sample



## CAT Simulation result




Residual stress resulting from welding process simulation.

## CAT Lap joint sample experimental plan

- Welding model validation
- Simple sample "representative" of a real weld
- 1/4" steel plate
- Monochromatic reflection geometry
- Traditional $\sin ^{2} \Psi$ analysis
- Replicate lab source experiment
- Vary energy
- CHESS F2

- Polychromatic Energy Dispersive Diffraction (EDD) m
- Penetrate through the plate
- Interrogate surface layer
- Plane stress - rosette analysis
- Advanced Photon Source (APS)

Mach, et. al.,JOM, 69:5, 393-399, 2017.

## Summarv of CAT Results



Mach, et. al.,JOM, 69:5, 393-399, 2017.

## Additive Manufacturing: Residual Stress and Distortion

Distortion Example (Blown Powder)

## Optomec LENS MR-7



## Residual Stress Induced Cracking

Powder Bed: EOS
 x W x H)
Substrate: Ti-6Al-4V, 4 in. $x 1$ in. $x 0.5$ in. ( $\mathrm{L} \times \mathrm{W} \times \mathrm{H}$ )
Courtesy Fred Lia and Wesley Mitchell
CIMP 3D, Penn State Univ.
\& Jim Williams - Ohio State Univ.

## Residual Stresses in AM Materials

- Monochromatic powder
- Measure gradient
- Map strain over thin flange
- Scans on grid of $0.5 \times 0.5 \mathrm{~mm}$
- 3600 Measurements!
- Thin section of sample
- Plane Stress
- Sample rotated 180 degrees about $y$-axis
- Stress result is average of "front" and "back" data.
- White beam measurements
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## Additive Manufacturing: Results

- [11 10$]$ reflection used to compute strain, with diffraction ring broken up into 10 degree arcs (for peak fitting).
- Isotropic Elasticity applied to calculate stress: $\mathrm{E}=114 \mathrm{GPa}, \mathrm{v}=0.342$
- Boundary conditions were used to adjust lattice parameter, adjusting so that normal stresses at corners are zero.



## Detectors - new speeds and ranges



## Brazing - 2 milliseconds



MM-PAD Detector: Sol Gruner, Cornell

- 150 micron pixels
- $38 \mathrm{~mm} \times 57 \mathrm{~mm}$
- (Left) $10^{7} \mathrm{x}$-rays / second; dynamic range 1-106 photons
- (Right) Seeing $\mathrm{Al}_{3} \mathrm{Ni}$ Debye rings with 5 photon range
- CdTe for high energy


## MM-PAD

## Detector

Tate et. al, Journal of
Physics: Conference
Series, 425(6): 062004, 2013.
Giewekemeyer et. al, J. Synch. Rad 21(5): 1167-1174, Sep 2014.

## CHESS-U Stations MSN-C Beamlines



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