# **Coherent Diffraction Imaging**

Ross Harder 34-ID-C Advanced Photon Source Acknowledgments: Prof. Ian Robinson (BNL) Dr. Xiaojing Huang (BNL) Dr. Jesse Clark (<del>PULSE institute, SLAC</del> Amazon) Prof. Oleg Shpyrko (UCSD) Dr. Andrew Ulvestad (<del>ANL – MSD</del>Tesla) Dr. Ian McNulty (<del>ANL – CNM</del> MaxIV) Dr. Junjing Deng (ANL – APS)



#### Non-compact samples (Ptychography)





#### High resolution imaging of structure, beyond optics.

Coherent beam scatters from sample. (Various contrast mechanisms) Measure modulus of Fourier Transform (Intensities). Use computational algorithms to retrieve phases. Recover image by Inverse Fourier Transform.





Visibility of fringes is a direct measure of the coherence of a beam. If beam is coherent across the spacing of the slits a Fourier Transform of the slit structure is observed downstream.



### COHERENCE

#### longitudinal coherence





### COHERENCE





# Coherence: Laser Speckle





A. L. Schawlow "Laser Light" Scientific American, 219 (3), p. 120, (1968)

Laser Speckle: Interference pattern arising from randomly distributed scatterers



### SIMPLEST SPECKLE EXPERIMENT: TWINKLE, TWINKLE LITTLE STAR



Stars are big, but very far away. As a result, their light has a high transverse coherence. As the light propagates through the atmosphere our eye detects a portion of the coherent diffraction



Courtesy Prof. Oleg Shpyrko (UCSD)

### First Speckle: Exner, 1877 (using candle light)



K. Exner: Sitzungsber. Kaiserl. Akad. Wiss. (Wien) 76, 522 (1877)

### First Speckle Photo: von Laue, 1914 (using arc discharge lamp)



M. von Laue: Sitzungsber. Akad. Wiss. (Berlin) 44, 1144 (1914) Argonne



 $I \propto \left| F(q) \right|^2$ 

#### First X-ray Speckle: M. Sutton et al., *Nature* **352**, 608-610 (1991)



FIG. 4 Speckle patterns measured using a 2.5- $\mu$ m, b, 5  $\mu$ m and c, 50- $\mu$ m collimating pinholes. The analysing pinholes used were 50, 25 and 100  $\mu$ m, respectively. Representative error bars are indicated, and the solid lines simply connect the data points. The (001) Bragg angle,  $2\theta_{\rm B}$ , is ~23.9°.



### WHY USE SYNCHROTRON RADIATION?

Synchrotron sources offer:

- Brightnesss (small source, collimated)
- Tunability (IR to hard x-rays)
- Polarization (linear, circular)
- Time structure (short pulses)

# Source brightness is the key figure of merit for coherent imaging







#### **B** = photons/source area, divergence, bandwidth

 $F_c \sim \lambda^2 B$ 



### **COHERENT X-RAY REFERENCES**

- Vartanyants, I A, and A Singer. 2010 "Coherence Properties of Hard X-Ray Synchrotron Sources and X-Ray Free-Electron Lasers." *New Journal of Physics* 12 (3): 035004.
- Singer, Andrej, and Ivan A Vartanyants. 2014. "Coherence Properties of Focused X-Ray Beams at High-Brilliance Synchrotron Sources." *Journal of Synchrotron Radiation* 21 (1). International Union of Crystallography: 5–15. doi:10.1038/nnano.2008.246.
- Nugent, Keith. 2009. "Coherent Methods in the X-Ray Sciences." Advances in Physics 59 (1): 1–99. doi:doi: 10.1080/00018730903270926.



### X-RAYS, TWO EXTREMES FOR STRUCTURAL STUDY:

X-ray Imaging (Shadowgraphs)



- Inhomogeneous, non-periodic materials
- Limited spatial resolution (~0.001 mm)



Roentgen, Nobel 1900

- Is particularly sensitive to periodicity in the sample (Crystals)
- Atomic resolution (unit cell)



Von Laue, Nobel 1914 Bragg & Bragg, Nobel 1915 Argonne



### **IMAGING REGIMES WITH COHERENT X-RAYS**





### **REFRACTIVE INDEX AND CONTRAST IN THE X-RAY REGION**

$$n = 1 - \delta - i\beta = 1 - \frac{r_e}{2\pi}\lambda^2 \sum_i n_i f_i(0)$$

$$A = A_0 \exp(-inkt)$$
$$k = 2\pi / \lambda$$

(C)

4

150

20

0

x (µm)







Diaz, Ana, et al, 2012. "Quantitative X-Ray Phase Nanotomography." Physical Review B 85.



21.7 μm

10 12 0

Argonne -

8

x (µm)

δ

6

(d) 6

s (mu)

10 12

10×10<sup>-6</sup>

### **REFRACTIVE INDEX AND CONTRAST IN THE X-RAY REGION** $n = 1 - \delta - i\beta = 1 - \frac{r_e}{2\pi} \lambda^2 \sum n_i f_i(0)$ $A = A_0 \exp(-inkt)$ $k = 2\pi/\lambda$



A. Diaz, et al., Journal of Structural Biology, vol. 192, no. 3, pp. 461–469, Oct. 2015.

Absorption contrast: sensitive to Im(n)~  $4\pi\beta(x,y)t/\lambda$  Phase contrast: sensitive to Re(n)~  $2\pi\delta(x,y)t/\lambda$ 



LD SP

S

Ν

R GC

# MAGNETIC CONTRAST IN FEGD



A. Tripathi, O.S. et al., Proc Natl Acad Sci USA 108, 13393 (2011)



### CDI IN BRAGG GEOMETRY: IMAGING DISPLACEMENT FIELD (STRAIN)



Coherent X-ray Diffraction measures:

$$\widetilde{\rho}(\mathbf{r}) = \rho_{\mathbf{G}_{hkl}}(\mathbf{r}) \exp\left[-i\mathbf{G}_{hkl} \cdot \mathbf{u}(\mathbf{r})\right]$$

Strain is a gradient of u(r), the phase component of the complex-valued density

Courtesy Prof. Oleg Shpyrko (UCSD)

### TRADITIONAL MICROSCOPY:





### **FIRST DEMONSTRATION OF CDI WITH X-RAYS**



diffraction pattern

reconstruction



### **COHERENT DIFFRACTIVE IMAGING:**





### PIXEL ARRAY DETECTORS: REVOLUTIONIZING COHERENT IMAGING



D. Schuette, S. Gruner (Cornell)

#### A Three Layer Hybrid Device

- Diode layer → converts x-rays to photocurrent.
- ASIC layer → custom signal processing electronics.
- A layer of metallic interconnects (bump bonds) between corresponding pixels on the diode and ASIC layers.

PADs can be read out in ~1 ms (CCDs take seconds!)

```
PAD pixels are 55-150 μm.
(CCDs are 12-24 μm)
```



Pilatus 6M detector (PSI/Dectris)



### **Coherent Diffraction from Crystals**





### **Coherent Diffraction from Crystals**





### Measuring 3D CXD



#### Silver Nano Cube (111)





Yugang Sun and Younan Xia, Science 298 2177 (2003)



### 3D Ag Nano Cube









Yugang Sun and Younan Xia, Science 298 2177 (2003)





#### APS 34-ID-C





#### Precision scanning stage



#### ORIGINAL PHASE RETRIEVAL PAPER (BY D. SAYRE):

Acta Cryst. (1952). 5, 843

#### **NOT** $\rho = \rho^2$ Acta Cryst. (1952). 5, 60

Some implications of a theorem due to Shannon. By D. SAYRE, Johnson Foundation for Medical Physics, University of Pennsylvania, Philadelphia 4, Pennsylvania, U.S.A.

(Received 3 July 1952)

Shannon (1949), in the field of communication theory, has given the following theorem: If a function d(x) is known to vanish outside the points  $x = \pm a/2$ , then its Fourier transform F(X) is completely specified by the values which it assumes at the points  $X = 0, \pm 1/a, \pm 2/a, \ldots$  In fact, the continuous F(X) may be filled in merely by laying down the function  $\sin \pi a X/\pi a X$  at each of the above points, with weight equal to the value of F(X) at that point, and adding.

Now the electron-density function d(x) describing a single unit cell of a crystal vanishes outside the points  $x = \pm a/2$ , where a is the length of the cell. The reciprocal-lattice points are at  $X = 0, \pm 1/a, \pm 2/a, \ldots$ , and hence the experimentally observable values of F(X)would suffice, by the theorem, to determine F(X) everywhere, if the phases were known. (In principle, the necessary points extend indefinitely in reciprocal space, but by using, say, Gaussian atoms both d(x) and F(X)can be effectively confined to the unit cell and the observable region, respectively.)

For centrosymmetrical structures, to be able to fill in the  $|F|^2$  function would suffice to yield the structure, for sign changes could occur only at the points where  $|F|^2$  vanishes. The structure corresponding to the  $|F|^2$ function is the Patterson of a single unit cell. This has twice the width of the unit cell, and hence to fill in the  $|F|^2$  function would require knowledge of  $|F|^2$  at the half-integral, as well as the integral h's. This is equivalent to a statement made by Gay (1951).

I think the conclusions which may be stated at this point are:

1. Direct structure determination, for centrosymmetric structures, could be accomplished as well by finding the sizes of the  $|F|^2$  at half-integral h as by the usual procedure of finding the signs of the F's at integral h.

2. In work like that of Boyes-Watson, Davidson & Perutz (1947) on haemoglobin, where  $|F|^2$  was observed at non-integral h, it would suffice to have only the values at half-integral h.

The extension to three dimensions is obvious.

#### References

- BOYES-WATSON, J., DAVIDSON, E. & PERUTZ, M. F. (1947). Proc. Roy. Soc. A, 191, 83.
- GAY, R. (1951). Paper presented at the Second International Congress of Crystallography, Stockholm.
- SHANNON, C. E. (1949). Proc. Inst. Radio Engrs., N.Y. 37, 10.

# Critical sampling



**FFT Real Part** 5 4.5 4 3.5 3 2.5 2 1.5 0.5 0 -0.5 100 110 120 130 140 150 160

### N unknown densities N/2 equations

$$\left|A_{q}\right| = \left|\sum_{0}^{N} \rho_{n} e^{-iqr_{n}}\right|$$

Nyquist Freq = 1/(2\*bandwidth) Intensity is under sampled



# Oversampling 2x



N/2 equations N/2 Unknown densities N/2 Known Densities(zero)

$$\left|A_{q}\right| = \left|\sum_{0}^{N} \rho_{n} e^{-iqr_{n}}\right|$$







R. W. Gerchberg and W. O. Saxton *Optik* <u>35</u> 237 (1972) Fienup, James R. 2013. "Phase Retrieval Algorithms: a Personal Tour." *Applied Optics* 52 (1). 56.







Harder, R., Liang, M., Sun, Y., Xia, Y., & Robinson, I. K. (2010). Imaging of complex density in silver nanocubes by coherent x-ray diffraction. *New Journal of Physics*, *12*(3), 035019.
 Huang, X., Harder, R., Xiong, G., Shi, X., & Robinson, I. (2011). Propagation uniqueness in three-dimensional coherent diffractive imaging. *Physical Review B*, *83*(22), 224109.



Harder, R., Liang, M., Sun, Y., Xia, Y., & Robinson, I. K. (2010). Imaging of complex density in silver nanocubes by coherent x-ray diffraction. *New Journal of Physics*, *12*(3), 035019.
 Huang, X., Harder, R., Xiong, G., Shi, X., & Robinson, I. (2011). Propagation uniqueness in three-dimensional coherent diffractive imaging. *Physical Review B*, *83*(22), 224109.

### Monitor Reciprocal Space Error











### **GENETIC/GUIDED ALGORITHM**



Clark, J. N., Ihli, J., Schenk, A. S., Kim, Y.-Y., Kulak, A. N., Campbell, J. M., et al. (2015). Three-dimensional imaging of dislocation propagation during crystal growth and dissolution. *Nature Materials*, *14*(8), 780–784. http://doi.org/10.1038/nmat4320

Clark, J. N., Huang, X., Harder, R., & Robinson, I. K. (2012). High-resolution three-dimensional partially coherent diffraction imaging. *Nature Communications*, *3*, 993–. http://doi.org/10.1038/ncomms1994


#### Ptychography (to fold) - Scanning CDI for extended object





#### Ptychography (to fold) - Scanning CDI for extended object





#### Ptychography (to fold) - Scanning CDI for extended object





#### Ptychography

#### diffraction pattern 4 Y(r)V(r)V(r)FFT $FFT^{1}$ O(r)diffraction pattern 3 diffraction pattern 2

Ptychographic iterative engine (PIE) J. Rodenburg *et al., PRL* **98**, 034801 (2007)

Exit surface wave field:  $\psi(r) = P(r)O(r)$ 

$$O(\mathbf{r}) = \frac{\sum_{j} P^{\star}(\mathbf{r} - \mathbf{r}_{j})\psi_{j}(\mathbf{r})}{\sum_{j} |P(\mathbf{r} - \mathbf{r}_{j})|^{2}} \quad P(\mathbf{r}) = \frac{\sum_{j} O^{\star}(\mathbf{r} + \mathbf{r}_{j})\psi_{j}(\mathbf{r} + \mathbf{r}_{j})}{\sum_{j} |O(\mathbf{r} + \mathbf{r}_{j})|^{2}}$$

P. Thibault et al., Science **321**, 379 (2008)

#### Platinum nanostructure



Spatial resolution: 
$$\delta = \frac{\lambda}{\theta} = \frac{\lambda z}{N\Lambda}$$



Courtesy Dr. Junjing Deng (APS)

ROSS J. HARDER (XSD) MATHEW J. CHERUKARA (XSD) YOUSSEF NASHED (MCS) TOM PETERKA (MCS) PRASANNA BALAPRAKASH (MCS) S. SANKARANARAYANAN (CNM) BADRI NARAYANAN (MSD)

A.I. CDI Atomistically Informed Coherent Diffraction Imaging



# **'PHYSICS-AWARE' NETWORK ARCHITECTURE**

- Common encoder to a latent space, two decoders to predict structure and phase.
  - 2D or 3D convolutions
- During training goal is to minimize the prediction error.
- Prediction error has 3 terms:
  - Error in object prediction
  - Error in phase prediction
  - Error in computed diffraction.
    - This is computed from the FT of predicted shape and phase.



M. J. Cherukara, et al.,

"Real-time coherent diffraction inversion using deep generative networks," Sci Rep, vol. 8, no. 1, p. 16520, Nov. 2018.

Yao, Yudong, et al..

"AutoPhaseNN: Unsupervised Physics-Aware Deep Learning of 3D Nanoscale Bragg Coherent Diffraction Imaging." Npj Computational Materials 8, no. 1 (June 3, 2022): 1–8.. Argonne

#### NEURAL NETWORK THAT LEARNS IMAGE RECONSTRUCTION



M. J. Cherukara, et al.,

"Real-time coherent diffraction inversion using deep generative networks," Sci Rep, vol. 8, no. 1, p. 16520, Nov. 2018.

# 3D Ag Nano Cube









Yugang Sun and Younan Xia, Science 298 2177 (2003)







Nature Materials 9, 120 - 124 (2010)

## 3D Strain Map in ZnO (0,0,c) Crystal-Bragg reflected X-ray beam Incident X-ray beam X $\xi_{ji} = (q_{kj}q_{ki})^{-1}$ $u_j = \xi_{ji} q_{ki} \phi_k;$ У N N γ. 1

Nature Materials 9, 120 - 124 (2010)

0.09 nm

0.0

1 1 1

1 1

# 3D Strain Map in ZnO



Nature Materials 9, 120 - 124 (2010)





Ultrafast three dimensional imaging of lattice dynamics in individual gold nanocrystals
J. N. Clark, L. Beitra, G. Xiong, A. Higginbotham, D. M. Fritz, H. T. Lemke, D. Zhu,
M. Chollet, G. J. Williams, M. Messerschmidt, B. Abbey, R. J. Harder,
A. M. Korsunsky, J. S. Wark & I. K. Robinson. (2013). *Science*, *341*(6141), 56–59





Ultrafast three dimensional imaging of lattice dynamics in individual gold nanocrystals J. N. Clark, L. Beitra, G. Xiong, A. Higginbotham, D. M. Fritz, H. T. Lemke, D. Zhu, M. Chollet, G. J. Williams, M. Messerschmidt, B. Abbey, R. J. Harder, A. M. Korsunsky, J. S. Wark & I. K. Robinson. (2013). *Science*, *341*(6141), 56–59



## Making ptychography colorful

Combination of Ptychography & Fluorescence



J. Deng, et al. PNAS 112, 2314-2319 (2015)

- Frozen-hydrated samples: closer to natural state, reduce radiation damage
- Fluorescence: quantitative elemental composition
- Ptychography: structure information with high resolution





- Frozen-hydrated *Chlamy.* Alga
- Ptychographic image resolution: ~18 nm
- Fluorescence image resolution:~ 100 nm
- Complementary information helps with sample analysis

J. Deng, et al.,

"X-ray ptychographic and fluorescence microscopy of frozen-hydrated cells using continuous scanning.," Sci Rep, vol. 7, no. 1, p. 445, Mar. 2017.



- Frozen-hydrated Chlamy. Alga
- Ptychographic image resolution: ~18 nm
- Fluorescence image resolution:~ 100 nm
- Complementary information helps with sample analysis

J. Deng, et al.,

"X-ray ptychographic and fluorescence microscopy of frozen-hydrated cells using continuous scanning.," Sci Rep, vol. 7, no. 1, p. 445, Mar. 2017.



#### **Extended to 3D**



Courtesy Dr. Junjing Deng (APS)



# **SURFACE DIFFRACTION COHERENT IMAGING**

- Image local surface structure
- Steps and step dynamics during film growth or interfacial reactivity
- Nanoparticle nucleation •
- Defect distributions, particularly at interfaces •
- Combined with x-ray micro fluorescence.....



(a) CCD

C. Zhu, et al. Applied Physics Letters, vol. 106, no. 10, p. 101604, Mar. 2015.

2.5

(b) recon. phase

# **APPLY FOR COHERENT IMAGING BEAMTIME @ APS!**



Email: Ross Harder rharder@aps.anl.gov https://wiki-ext.aps.anl.gov/s34idc/index.php/34-ID-C

#### Bragg Ptychography



Email: Martin Holt mvholt@anl.gov https://wiki-ext.aps.anl.gov/s26id/index.php/26-ID

# Ptychography Tomography Email: Junjing Deng junjingdeng@aps.anl.gov

## https://www.aps.anl.gov/Users-Information



#### Feedback Lecture – 11:00 – 12:00 Coherence Based Imaging - Ross Harder https://forms.office.com/g/52JJbFGggP





## SUPPLEMENTAL SLIDES



#### LARGE-FORMAT, SINGLE-PHOTON SENSITIVE X-RAY CCD CAMERAS OPENED THE DOOR TO COHERENT X-RAY IMAGING

Fairchild Peregrine 486 CCD Camera

- 4K x 4K pixel array (61.4 mm square area)
- 15 µm pixels, 100% fill factor
- Back-illuminated for up to 80% QE
- Readout noise < 5 e- at 50 Kpixels/s
- Dynamic range > 86 dB in MPP
- 6 s readout with four on-chip amplifiers
- Pixel binning for more rapid readout
- Peltier-cooled to -50 C for low dark current





## Hi Resolution Imaging (CCD)?





#### At APS 34-ID-C: 9.25 hours of scanning 38 minutes of x-ray exposure

Rainbow color map (still) considered harmful http://ieeexplore.ieee.org/document/4118486/



# Patterned Gold Nanocystal Samples







(11-1)





(11-1)





(11-1)





→ -111



(-111)

11-1

-111













# Vector Displacement Field of Gold lattice



Produced by combining reconstructions from (11-1) (020) (-111)



Ptychographic spectroscopy

-- like STXM XNEAS analysis, but with higher resolution and more information (both absorption and phase) from refractive index











A. Tripathi, O.S. et al., Proc Natl Acad Sci USA 108, 13393 (2011)


 58.5 mT
 76.5 mT
 96.5 mT

 A. Tripathi, O.S. et al., Proc Natl Acad Sci USA 108, 13393 (2011)

### Hi Resolution Imaging (PAD)?



Quad Timepix GaAs sensor

700nm gold crystal
3 degree rocking curve
25 minute measurement
15 sec movie (1X APS-U measurement)







#### Equipment for In-situ BCDI at APS 34-ID-C Beamline



#### **Cooling Chamber**



#### **Heating Chamber 2**



#### **Gas/Liquid Flow Cell**







Argonne 🛆

#### **EXPERIMENT**

#### alignment of tip to X-ray





### At which plane ptychographic images are reconstructed $\psi(r) = P(r)O(r)$

Ptychography always produces images at the sample plane.



#### PTYCHOGRAPHY MICROPROBES -> COHERENT IMAGING INSTRUMENT





Vine, et al. (2012). Opt. Express, 20(16), 18287–18296.



# GDFE LAYERED MAGNETIC FILMS



# MAGNETIC CONTRAST MECHANISM



Argonne

### REAL SPACE RECONSTRUCTION



(exit wave Tripathi, O.S. et al., Proc Natl Acad Sci USA 108, 13393 (2011)

## REAL SPACE RECONSTRUCTION



Magnetic structure Illumination Function (exit wave)

A. Tripathi, O.S. et al., Proc Natl Acad Sci USA 108, 13393 (2011)